

# cDMN: Combining DMN with Constraint Reasoning

## DecisionCAMP2020

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**KU LEUVEN**



# OUTLINE

1. DMN
2. Constraint DMN
3. cDMN application: Doctor Planning
4. Comparison to other solutions
5. A user friendly pipeline from cDMN to interface



# DMN

## What DMN does well:

- Very readable
- Very intuitive
- Easy to formalize decision making

# DMN

However: not well-suited for complex decision making:

- FEEL: can express a lot, but becomes unreadable
- No constraints
- No optimization

→ we propose additions to overcome these limitations.



# WHAT IS cDMN?

## cDMN: constraint DMN

- Extends DMN with constraint reasoning
- Quantification, types, functions, relations, optimization, ..
- Model complex decisions
- Introduces new tables
  - Glossary
  - Constraint tables
  - Data tables
  - Execute tables

# THE GLOSSARY

## Changes in representation:

- DMN: constants
- cDMN: types, functions, relations, constants, booleans  
→ defined by glossary



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Name	Type	Values
Person	string	Agatha, Butler, Charles
Number	int	[0..100]

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Name	
Person hates Person	
Person is richer than Person	

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Name	
Suicide	

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Boolean
Name
Suicide

Constant	
Name	Type
Killer	Person

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Person	string	Agatha, Butler, Charles
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Relation	
Name	
Person hates Person	
Person is richer than Person	

Boolean	
Name	
Suicide	

Constant	
Name	Type
Killer	Person

Function	
Name	Type
Age of Person	Number
Hates of Person	Number

# CONSTRAINT TABLES

Constraint tables differ in two ways from decision tables:

- 1 Outputs can contain S-FEEL.
- 2 Rows express *logical implications*:
  - IF input satisfied, THEN output has to be satisfied
  - Nothing said about output when no input applicable (no Null)

**E\*** hit policy

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E\* hit policy

Nutritional values				
E*	RequireHealthy	Total Sodium	Total Fat	Total Calories
1	Yes	<3000	<150	<3000

$RequireHealthy \Rightarrow TotalSodium < 3000 \wedge TotalFat < 150 \wedge TotalCalories < 3000$

# QUANTIFICATION

cDMN also allows *universal quantification*:

- Logic for all values of a type
- Type as column header
- Subsequent uses refer to the quantified variable.



# CONSTRAINTS AND QUANTIFICATION: EXAMPLE

Example:

Noone hates all		
E*	Person	Hatees of Person
1	-	< 3

$$\forall Person[Person] : Hatees(Person) < 3$$

# CONSTRAINTS AND QUANTIFICATION: EXAMPLE

## Example:

Noone hates all		
E*	Person	Hatees of Person
1	-	< 3

$$\forall Person[Person] : Hatees(Person) < 3$$

Bordering countries can not share colors				
E*	Country called c1	Country called c2	c1 and c2 are Bordering	Color of c1
1	-	-	Yes	Not(Color of c2)

$$\forall c1[Country], c2[Country] : Bordering(c1, c2) \Rightarrow Color(c1) \neq Color(c2)$$

# DATA TABLES

Typically, problems can be split up in two parts:

- 1 general logic of the problem
- 2 specific problem instance to solve

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Map coloring problem:

- 1 Two bordering countries cannot share a color.
- 2 The specific map to color (e.g. Western Europe).

# DATA TABLES

**Logic:** decision and constraint tables  
**Problem instance:** data tables

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- Only basic values
- Quantification possible

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**Logic:** decision and constraint tables

**Problem instance:** data tables

- No hit policy, but "Data Table" in name
- Only basic values
- Quantification possible

Data Table: Declaring which countries border			
	Country called c1	Country called c2	c1 and c2 are Bordering
1	Belgium	France, Luxembourg, Netherlands, Germany	Yes
2	Germany	France, Denmark, Luxembourg, Belgium, Netherlands	Yes
	...	...	Yes

# MODEL SOLVING AND OPTIMIZATION

- DMN always has a single solution for a set of inputs
- not the case in cDMN
  - cDMN defines solution space
- *Execute table* specifies solutions



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<b>Execute</b>
Get 1 model

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Execute
Get 1 model

Execute
Get all models

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- *Execute table* specifies solutions

Execute
Get 1 model

Execute
Get all models

Execute
Maximize Score



# CHALLENGE SPECIFICATION

## Doctor Planning

- Doctor present at all times in a hospital
- Planning made per week
- Days consist of three shifts (early, late, night)
- Five doctors in total
- Each doctor has different availabilities

# CHALLENGE SPECIFICATION: RULES

## Rules

- 1 A doctor can only work one shift per day.
- 2 A doctor should always be available for his shift (see table below).
- 3 If a doctor has the night shift, they either get the next day off, or the night shift again.
- 4 A doctor either works both days of the weekend, or none of the days.

# CHALLENGE SPECIFICATION: AVAILABILITIES

## Availabilities

Name	Available
Fleming	Friday, Saturday, Sunday
Freud	Every day early or late, never night
Heimlich	Every day but never the night shift on weekends
Eustachi	Every day, every shift
Golgi	Every day, every shift but at max 2 night shifts

A planning should be made in which every requirement is fulfilled.

# DOCTOR PLANNING: RULES

## Rule 1

A doctor can only work one shift per day.

Type		
Name	Type	Values
Doctor	string	Fleming, Freud, Heimlich, Eustachi, Golgi
Day	string	Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday
Nb Shift	int	[0..21]

Function	
Name	Type
Nb Shifts of Doctor and Day	Nb Shift



# DOCTOR PLANNING: RULES

## Rule 1

A doctor can only work one shift per day.

Rule 1			
E*	Doctor	Day	Nb Shifts of Doctor and Day
1	-	-	$\leq 1$

# DOCTOR PLANNING: RULES

## Rule 2

A doctor should be available for his shift.

Type		
Name	Type	Values
Doctor	string	Fleming, Freud, Heimlich, Eustachi, Golgi
Day	string	Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday
Nb Shift	int	[0..21]
Shift_Type	string	Early, Late, Night

Function	
Name	Type
Nb Shifts of Doctor and Day	Nb Shift
Assigned Doctor of Day and Shift_Type	Doctor

Relation
Name
Available Doctor for Shift_Type and Day

# DOCTOR PLANNING: RULES

## Rule 2

A doctor should be available for his shift.

Rule 2					
E*	Doctor	Day	Shift_Type	Assigned Doctor of Day and Shift_Type	Available Doctor for Shift_Type and Day
1	-	-	-	Doctor	Yes

# DOCTOR PLANNING: RULES

## Rule 3

If a doctor has the night shift, they either get the next day off, or the night shift again.

Type		
Name	Type	Values
Doctor	string	Fleming, Freud, Heimlich, Eustachi, Golgi
Day	string	Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday
Nb Shift	int	[0..21]
Shift_Type	string	Early, Late, Night

Function	
Name	Type
Nb Shifts of Doctor and Day	Nb Shift
Assigned Doctor of Day and Shift_Type	Doctor
Next_Day of Day	Day

Relation
Name
Available Doctor for Shift_Type and Day

# DOCTOR PLANNING: RULES

## Rule 3

If a doctor has the night shift, they either get the next day off, or the night shift again.

Rule 3							
E*	Doctor	Day called d1	Shift_Type called s1	Doctor of d1 and s1	Day called d2	Shift_Type called s2	Doctor of d2 and s2
1	-	-	Night	Doctor	Next_Day of d1	Early, Late	not(Doctor)

# DOCTOR PLANNING: RULES

## Rule 4

A doctor either works both days of the weekend, or none of the days.

Type		
Name	Type	Values
Doctor	string	Fleming, Freud, Heimlich, Eustachi, Golgi
Day	string	Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday
Nb Shift	int	[0..21]
Shift_Type	string	Early, Late, Night

Function	
Name	Type
Nb Shifts of Doctor and Day	Nb Shift
Assigned Doctor of Day and Shift_Type	Doctor
Next_Day of Day	Day

Relation
Name
Available Doctor for Shift_Type and Day

# DOCTOR PLANNING: RULES

## Rule 4

A doctor either works both days of the weekend, or none of the days.

Rule 4					
E*	Doctor	Day called d1	Nb Shifts of Doctor and d1	Day called d2	Nb Shifts of Doctor and d2
1	-	Saturday	1	Sunday	1
2	-	Sunday	1	Saturday	1

# DOCTOR PLANNING: RULES

## Special Preference

Golgi works at maximum two nights.

Type		
Name	Type	Values
Doctor	string	Fleming, Freud, Heimlich, Eustachi, Golgi
Day	string	Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday
Nb Shift	int	[0..21]
Shift_Type	string	Early, Late, Night

Function	
Name	Type
Nb Shifts of Doctor and Day	Nb Shift
Assigned Doctor of Day and Shift_Type	Doctor
Next_Day of Day	Day
Nb Nights of Doctor	Nb Shift

Relation
Name
Available Doctor for Shift_Type and Day



# DOCTOR PLANNING: RULES

## Special Preference

Golgi works at maximum two nights.

Max Nights		
E*	Doctor	Nb Nights of Doctor
1	Golgi	$\leq 2$

# DOCTOR PLANNING: AVAILABILITIES

Data Table: Availabilities				
	Doctor	Shift_Type	Day_Type	Available Doctor for Shift_Type and Day
1	Fleming	Early	Friday	Yes
2	Fleming	Late	Friday	Yes
3	Fleming	Night	Friday	Yes
4	Fleming	Early	Saturday	Yes
	...	...	...	...

# DOCTOR PLANNING: OTHER TABLES

Next Day		
U	Day	Next_Day of Day
1	Sunday	Monday
2	Monday	Tuesday
3	Tuesday	Wednesday
4	Wednesday	Thursday
5	Thursday	Friday
6	Friday	Saturday
7	Saturday	Sunday

# DOCTOR PLANNING: OTHER TABLES

Next Day		
U	Day	Next_Day of Day
1	Sunday	Monday
2	Monday	Tuesday
3	Tuesday	Wednesday
4	Wednesday	Thursday
5	Thursday	Friday
6	Friday	Saturday
7	Saturday	Sunday

Count shifts per day					
C+	Doctor	Day	Shift_Type	Assigned Doctor of Day and Shift_Type	Nb Shifts of Doctor and Day
1	-	-	-	Doctor	1

# DOCTOR PLANNING: OTHER TABLES

Next Day		
U	Day	Next_Day of Day
1	Sunday	Monday
2	Monday	Tuesday
3	Tuesday	Wednesday
4	Wednesday	Thursday
5	Thursday	Friday
6	Friday	Saturday
7	Saturday	Sunday

Count shifts per day					
C+	Doctor	Day	Shift_Type	Assigned Doctor of Day and Shift_Type	Nb Shifts of Doctor and Day
1	-	-	-	Doctor	1

Count night shifts for every doctor					
C+	Doctor	Day	Shift_Type	Assigned Doctor of Day and Shift_Type	Nb Nights of Doctor
1	-	-	Night	Doctor	1

# DOCTOR PLANNING: FULL

Define Next Day	
U	Day
1	Monday
2	Tuesday
3	Wednesday
4	Thursday
5	Friday
6	Saturday
7	Sunday

Type		
Name	Data Type	Possible Values
Doctor	string	Fleming, Freud, Heimlich, Eustachi, Golgi
Shift_Type	string	Early, Late, Night
Day	string	Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday
Nb Shift	int	{0..21}

Function	
Name	Data Type
Assigned Doctor of Day and Shift_Type	Doctor
Day of Shift	Day
Nb Shifts of Doctor and Day	Nb Shift
Nb Nights of Doctor	Nb Shift
Next_Day of Day	Day

Relation	
Name	
Available Doctor for Shift_Type and Day	

Count shifts per day				
C+	Doctor	Day	Shift_Type	Assigned Doctor of Day and Shift_Type
1-	-	-	-	Doctor

1. A doctor can only work one shift per day

E*	Doctor	Day	Nb Shifts of Doctor and Day
1-	-	-	<= 1

2. A doctor should always be available for his shift.

E*	Doctor	Day	Shift_Type	Assigned Doctor of Day and Shift_Type	Available Doctor for Shift_Type and Day
1-	-	-	-	Doctor	Yes

3. If a doctor has the night shift, they either get the next day off, or the night shift again.

E*	Doctor	Day called d1	Shift_Type called s1	Assigned Doctor of d1 and s1	Day called d2	Shift_Type called s2	Assigned Doctor of d2 and s2
1-	-	-	Night	Doctor	Next_Day of d1	not(Night)	not(Doctor)

4. A doctor either works both days of the weekend, or none of the days.

E*	Doctor	Day called d1	Nb Shifts of Doctor and d1	Day called d2	Nb Shifts of Doctor and d2
1-	-	Saturday	1	Sunday	1
2-	-	Sunday	1	Saturday	1

Max Nb of Nights	
E*	Doctor
1	Golgi

Count the number of night shifts for each doctor

C+	Doctor	Day	Shift_Type	Assigned Doctor of Day and Shift_Type	Nb Nights of Doctor
1-	-	-	Night	Doctor	1

Data Table: available doctors			
Doctor	Shift_Type	Day	Available Doctor for Shift_Type and Day
1Fleming	Early	Friday	Yes
2Fleming	Late	Friday	Yes
3Fleming	Night	Friday	Yes
4Fleming	Early	Saturday	Yes



# COMPARISON

On 10th of June, these were the solutions:

- OPL (Alex Fleisher)
- PostgreSQL (Damir Sudarevic)
- ZIMPL (Rob Parker)
- Prolog (Matteo Redaelli)
- OpenRules, JavaSolver, AWS Lambda (Jacob Feldman)

None are DMN-like implementations.



# COMPARISON

OPL:

```
// night shift ==> next day off or next night shift  
  
forall(d in doctors,i in days:(i+1) in days)  
{  
    (x[d][i]["night"]==1) => (x[d][i+1]["early"]==0);  
    (x[d][i]["night"]==1) => (x[d][i+1]["late"]==0);  
}
```

# COMPARISON

## ZIMPL:

**# If a doctor works night shift, they cannot work early or late the next day...**

**subto Night\_Shift\_Continuity1:**

**forall <p> in PROFESSIONALS :**

**forall <d> in DAYS with d < 7:**

**vif (ASSIGNED[d,"Night",p] >= 1) then**

**ASSIGNED[d+1,"Early",p] <=0**

**end;**

**subto Night\_Shift\_Continuity2:**

# COMPARISON

## OpenRules, JavaSolver, AWS Lambda:

```
// If a doctor has the night shift,  
// they either get next day off or the the night shift again  
if (day > 0) {  
  if (shift < nightShift && !Doctor.FROZEN.equals(status)) {  
    Var previousNightShift = vars[doc][day - 1][nightShift];  
    Constraint constraint1 = csp.linear(previousNightShift, "=", 1);  
    Constraint constraint2 = csp.linear(var, "=", 0);  
    csp.postIfThen(constraint1, constraint2);  
  }  
}
```

# COMPARISON

## OpenRules, JavaSolver, AWS Lambda:

**Weekly Schedule**

Select an action: ☐ Assign ☒ Block ☐ Free


☐ ☒ ☐

Worker	Sun			Mon			Tue			Wed			Thu			Fri			Sat			Sun		
	1	2	3	1	2	3	1	2	3	1	2	3	1	2	3	1	2	3	1	2	3	1	2	3
Fleming																								
Freud																								
Heimlich																								
Eustachi																								
Golgi																								

# LIVE WORKER SCHEDULER

Jacob Feldman created a full-blown planning application

- The GUI is created using OpenRules Dialog
- The scheduling is implemented in JavaSolver
- + The GUI is very intuitive and the system works well
  - The solver is written in Java, only accessible to software developers



# 5 A USER FRIENDLY PIPELINE FROM CDMN TO INTERFACE

# AUTOCONFIG INTERFACE

Using the cDMN solver, a cDMN specification can be fed to the Autoconfig interface

- Users can interact with the cDMN specifications
- Users can set values, and see the results
- The system doesn't distinguish between inputs or outputs
- The system can find optimal solutions

# AUTOCONFIG INTERFACE DEMO

Autoconfig3

localhost:4201

## Doctor Planning

Edit File Visibility Collapse Relevance Notion Reset Choices Modelexpand Undo Modelexpand

### Assigned\_Doctor

Monday,Early

?	Fleming
✓	Freud
✓	Heimlich
✓	Eustachi
✓	Golgi

Monday,Late

?	Fleming
✓	Freud
✓	Heimlich
✓	Eustachi
✓	Golgi

Monday,Night

?	Fleming
?	Freud
✓	Heimlich
✓	Eustachi
✓	Golgi

Tuesday,Early

?	Fleming
✓	Freud
✓	Heimlich
✓	Eustachi

### Nb\_Nights

Fleming

✓	0
✓	1
✓	2
✓	3
?	4

Freud

?	0
?	1
?	2
?	3
?	4

Heimlich

✓	0
✓	1
✓	2
✓	3
✓	4

Eustachi

✓	0
✓	1
✓	2
✓	3

Version: v0.1.30-gf6d5f5-4nry





# ANY QUESTIONS?

For further questions or discussion:  
[s.vandeveld@kuleuven.be](mailto:s.vandeveld@kuleuven.be)

For more information on cDMN and the cDMN solver:  
[www.cdmn.be](http://www.cdmn.be)

For more information on the interface:  
<https://gitlab.com/krr/autoconfigz3>